

Bifacial Silicon (N+/P/P+) Silicon Solar Cell Base Thickness Optimization under Back Illumination of Long Wavelength: Effect of Diffusion Coefficient Resonance in Temperature under Applied Magnetic Field

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Abstract This work aims to save silicon material, for the realization of the solar cell, by reducing the thickness of the base. For this, the (n⁺/p/p⁺) silicon solar cell at temperature (T) is placed in a variable magnetic field (B) and back illuminated by a monochromatic light of deep penetration into the base. The magneto-transport equation relating to the density of the photogenerated carriers at depth in the base is solved and allows to extract the expressions of the recombination velocity on the rear side. A graphic technique of the study of these expressions in a situation of resonance of minority carriers diffusion, gives the optimum thickness of the base. The results obtained show a decrease in optimum thickness with both parameters, temperature and magnetic field. Mathematical modeling of these results, shows the possibility of making thin solar cells and saving silicon material

Keywords Silicon Solar Cell, Diffusion Coefficient, Resonance, Temperature, Magnetic field, Recombination Velocity, Absorption Coefficient, Base Thickness

1. Introduction

Improving the efficiency [1, 2] of silicon solar cells involves examining:

- i) Architecture such as monofacial [3], bifacial [4-9], multi-junction silicon [10, 11] (vertical or series) and thin films [12, 13]
- ii) Phenomological parameters [14 -24], which are: lifetime, diffusion length, mobility, which are related by the Einstein relation, as well as surface recombination, at the surface of the emitter, at the emitter-base (junction), at the back side of the base, and at the grain boundaries
- iii) The parameters of the model electrical equivalent to the solar cell in static mode [25-29], given by the series and shunt resistors, the capacitance of the space charge zone and the diffusion capacitance. In dynamic mode, ie transient decay [16, 17, 30, 31, 32] or impedance spectroscopy [33 - 38], it will be impedance, conductance and capacitance determination.



External factors influence the operation of the solar cell and must be taken into account, as they act on the elements mentioned above.

These are:

- 1) Illumination through it's: concentration [18, 35, 39], angle of incidence [40] and shading [41] produced, spectral quality (mono or polychromatic light) [42], its incident flux of constant amplitude [43], pulsed [16, 17, 31, 32] or with frequency modulation [15, 24, 44-46]
- 2) Effects of applied: temperature [47, 48, 49], electromagnetic field [14, 50-53], and irradiation by electrically charged particles [54, 55].

The concomitance of external factors can be imposed on the solar cell [38, 56-62].

The geometric parameters [21], which are the dimensions of the different regions that make up the solar cell, are also important for the analysis of the physical mechanisms that take place there [22]. This is the thickness of: the emitter [63], the space charge region [13, 64, 65] the base [23, 57, 58, 61, 66, 67] and also the grains size [21].

This work aims to save silicon material, for the realization of bifacial silicon solar cell, by reducing the thickness of the base and the production of maximum photocurrent, while phenomenological parameter, such as, diffusion coefficient gives high response i.e. in resonance [38, 59, 60, 61, 62, 66, 67].

For this, the bifacial silicon solar cell ($n^+/p/p^+$) at temperature (T) is placed in a variable magnetic field (B) and back illuminated by a monochromatic light of deep penetration into the base ($L < H < 1/\alpha$) [68, 69], i.e. reciprocal absorption coefficient (α) larger than both base thickness (H) and diffusion length (L).

The optimized thickness [2] in a condition of temperature resonance of the diffusion coefficient of the minority carriers [59], would lead to an optimization of the photocurrent delivered and a saving of material used in the manufacture of a bifacial solar cell.

2. Theory

The structure of the (n^+-p-p^+) bifacial silicon solar cell [4-9] under monochromatic illumination, under magnetic field B at temperature T , is shown by figure.1.

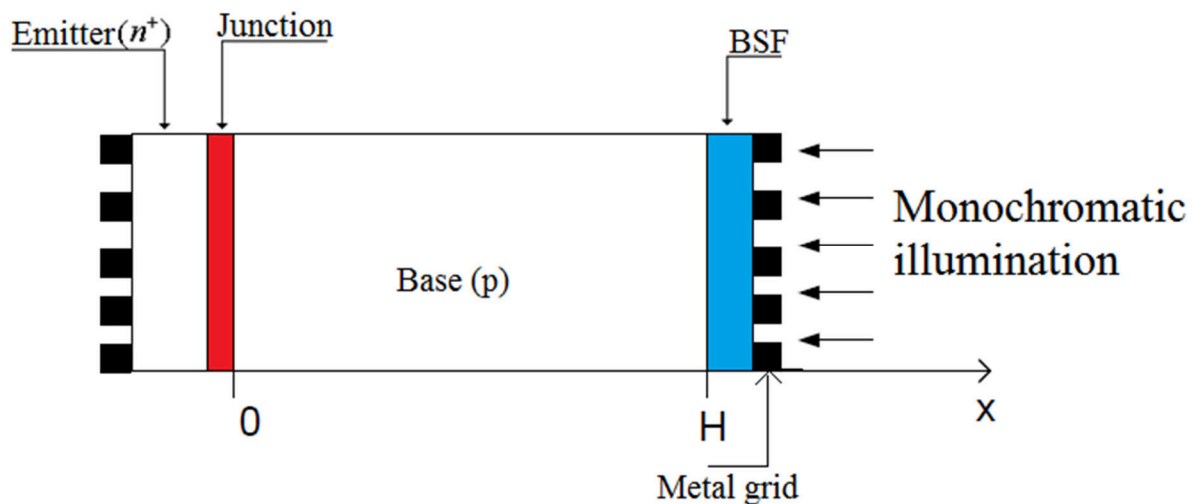


Figure 1: Structure of monofaciale solar cell

The generated excess minority carriers' density $\delta(x, B, T)$ at coordinate (x), in the base of the solar cell, under magnetic field B at temperature T , under monochromatic illumination, is governed by the following magneto transport equation in steady state [14, 50-53]:

$$D(B, T) \times \frac{\partial^2 \delta(x)}{\partial x^2} - \frac{\delta(x)}{\tau} = -G(x) \tag{1}$$

τ and $D(B, T)$ are respectively the lifetime and the diffusion coefficient of the excess minority carriers in the base under magnetic field and under temperature.

Under magnetic field, the diffusion coefficient is given by the following relation [50, 51]

$$D(B, T) = \frac{D(T)}{1 + (\mu B)^2} \tag{2}$$

With Einstein relation: $D(T) = \frac{\mu(T) \cdot K \cdot T}{q}$ (3)

The elementary charge of electron is q , and K is the Boltzmann constant.

And the mobility coefficient is given as temperature dependent [24, 49]:

$$\mu(T) = 1,43 \cdot 10^{19} \cdot T^{-2,42} \tag{4}$$

- L represents the excess minority carriers' diffusion length in the base:

$$L^2(B, T) = D(B, T) \cdot \tau \tag{5}$$

- The carrier generation rate $G(x)$ is given by the relationship [6, 9]:

$$G(x) = \alpha \cdot I_0 \cdot (1 - R) \cdot e^{-\alpha \cdot (H-x)} \tag{6}$$

The incident flux on the rear of the base is (I_0), (α) and (R) are the monochromatic absorption and reflection coefficients of the silicon material [17, 43, 68, 69].

The solution of equation (1) is:

$$\delta(x, \alpha, B, T) = A \cdot \cosh\left[\frac{x}{L(B, T)}\right] + E \cdot \sinh\left[\frac{x}{L(B, T)}\right] + K \cdot e^{-\alpha(H-x)} \tag{7}$$

With $K = -\frac{\alpha \cdot I_0 \cdot (1 - R) \cdot [L(B, T)]^2}{D(B, T) [L(B, T)^2 \cdot \alpha^2 - 1]}$ (8)

And $(L(B, T)^2 \cdot \alpha^2 \neq 1)$ (9)

Coefficients A and E are determined through the boundary conditions:

■ At the junction ($x = 0$)

$$\left. \frac{\partial \delta(x, \alpha, B, T)}{\partial x} \right|_{x=0} = S_f \cdot \left. \frac{\delta(x, \alpha, B, T)}{D(B, T)} \right|_{x=0} \tag{10}$$

■ On the back side in the base ($x = H$) (11)

$$\left. \frac{\partial \delta(x, \alpha, B, T)}{\partial x} \right|_{x=H} = -S_b \cdot \left. \frac{\delta(x, \alpha, B, T)}{D(B, T)} \right|_{x=H} \tag{12}$$



Sf and Sb are respectively the recombination velocities of the excess minority carriers at the junction [19, 32] and at the back surface [19, 20, 44, 45].

3. Results and Discussions

3.1 Diffusion coefficient at resonance

Combining equations 2, 3, 4, the optimum temperature (Topt) is obtained at the maximum (Dmax) of the curve D(B, T), for a given magnetic field (B). Thus the expression [59] is given by:

$$T_{Op}(B) = \sqrt[4]{2,4 \times (1,43 \cdot 10^9)^2 \cdot B^2} \tag{13}$$

This relationship allows to calculate the optimal temperature (Topt) for different values of the magnetic field (B) and to deduce the maximum diffusion coefficient (Dmax). **Table. 1** below shows the results achieved.

3.2 Photocurrent density

The photocurrent density at the junction is obtained from the density of minority carriers in the base and is given by the following expression:

$$J_{ph}(Sf, \alpha, B, T) = q \cdot D(B, T) \cdot \left. \frac{\partial \delta(x, \alpha, B, T)}{\partial x} \right|_{x=0} \tag{14}$$

Figure 2 shows photocurrent versus the junction surface recombination velocity for different diffusion coefficient (Dmax).

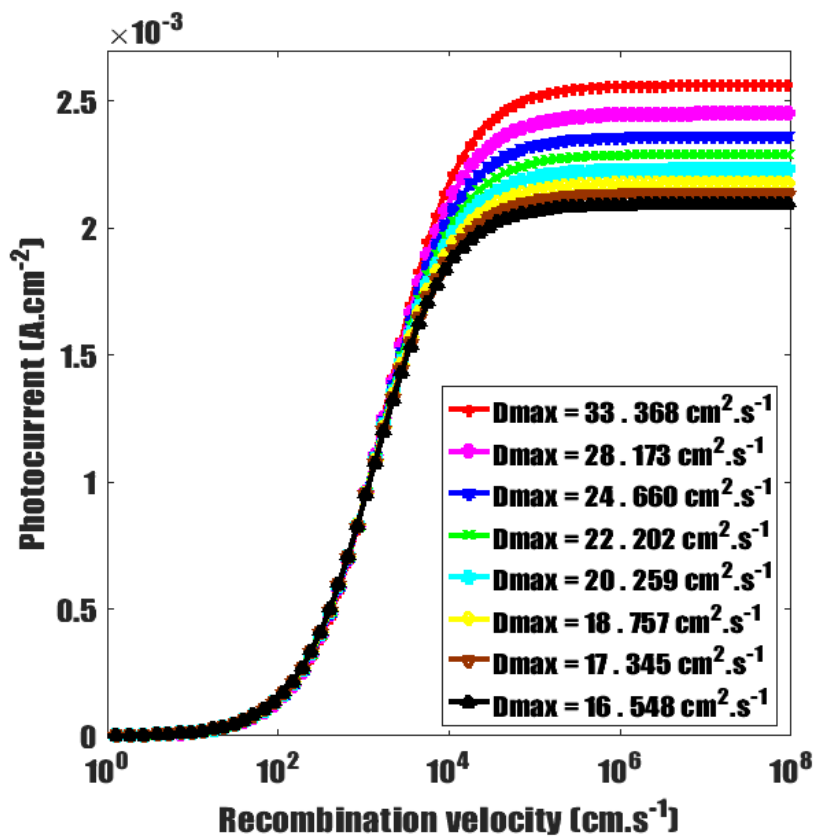


Figure 2: Photocurrent density versus recombination velocity for different diffusion coefficient ($\alpha = 6.2 \text{ cm}^{-1}$)

3.2 Base thickness optimization

The plotted photocurrent density versus (S_f) minority carriers' recombination velocity at the junction (Figure. 2), is marked by three zones [19, 70, 71]. At low recombination (S_f) velocity values, the carriers are locked at the junction, which corresponds to an open circuit operation, because the photocurrent density is zero. Then the photocurrent grows rapidly in the second region, to reach an asymptotic value in the third region, which is the short-circuit current density. This flat region is well marked whatever the values of the diffusion coefficient (D_{max}). The short-circuit current density increases with the diffusion coefficient, which decreases with optimum temperature and magnetic field (See Table. 1). The thermal agitation and deflection of the charge carriers, in high velocity, reduces the density of short-circuit photocurrent. From this situation of constant short-circuit current, it comes that:

$$\left. \frac{\partial J_{ph}(S_f, S_b, \alpha, H, B, T)}{\partial S_f} \right|_{S_f \geq 10^5 \text{ cm.s}^{-1}} = 0 \tag{15}$$

The solution of this equation leads to the mathematical expressions of the (S_b) recombination velocity of the minority carriers on the back side of the base, as:

$$S_{b1}(H, B, T) = -\frac{D(B, T)}{L(B, T)} \cdot \tanh\left(\frac{H}{L(B, T)}\right) \tag{16}$$

$$S_{b2}(H, \alpha, B, T) = \frac{D(B, T)}{L(B, T)} \cdot \left[\frac{L(B, T) \cdot \alpha - \left(L(B, T) \cdot \alpha \cdot \operatorname{ch}\left(\frac{H}{L(B, T)}\right) + \operatorname{sh}\left(\frac{H}{L(B, T)}\right) \right) e^{-\alpha H}}{\left(\operatorname{ch}\left(\frac{H}{L(B, T)}\right) + L(B, T) \cdot \alpha \cdot \operatorname{sh}\left(\frac{H}{L(B, T)}\right) \right) e^{-\alpha H} - 1} \right] \tag{17}$$

Figure 3 shows the application of the graphical technique [57, 58, 61, 72, 73] which makes it possible to deduce the optimum thickness of the base, by the intersection of the curves S_{b1} and S_{b2} , for every maximum diffusion coefficient (D_{max}) value, and for weak absorption coefficient ($\alpha(\lambda)$).

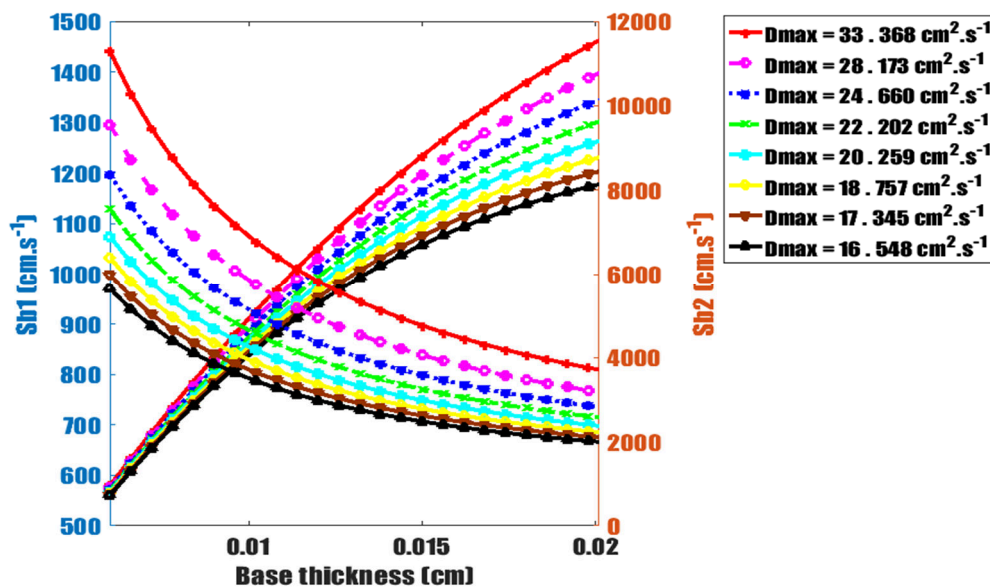


Figure 3: S_{b1} and S_{b2} versus depth in the base for different diffusion coefficient



The table. 1 gives the results extracted from the curves of figure. 3.

Table 1: Base optimum thickness obtained with maximum values of minority carriers’ diffusion coefficient and optimal temperature for different magnetic field values

Magnetic field B (T)	0.0003	0.0004	0.0005	0.0006	0.0007	0.0008	0.0009	0.001
Optimum temperature T_{opt} (K)	255	285	308	335	355	380	400	410
Maximum diffusion Coefficient D_{max} (cm^2/s)	33.364	28.178	24.694	22.206	20.276	18.763	17.571	16.642
Optimum thickness H_{opt} (cm)	0.0114	0.0108	0.0102	0.0099	0.0096	0.0093	0.0091	0.009

Extracted from the data in **Table 1**, **Figures 4, 5** and **6**, represent the optimum thickness of the base of the solar cell as a function respectively of the maximum diffusion coefficient of the minority carriers, the applied magnetic field and the temperature. **Equations 18, 19** and **20**, represent the mathematical modeling of these curves.

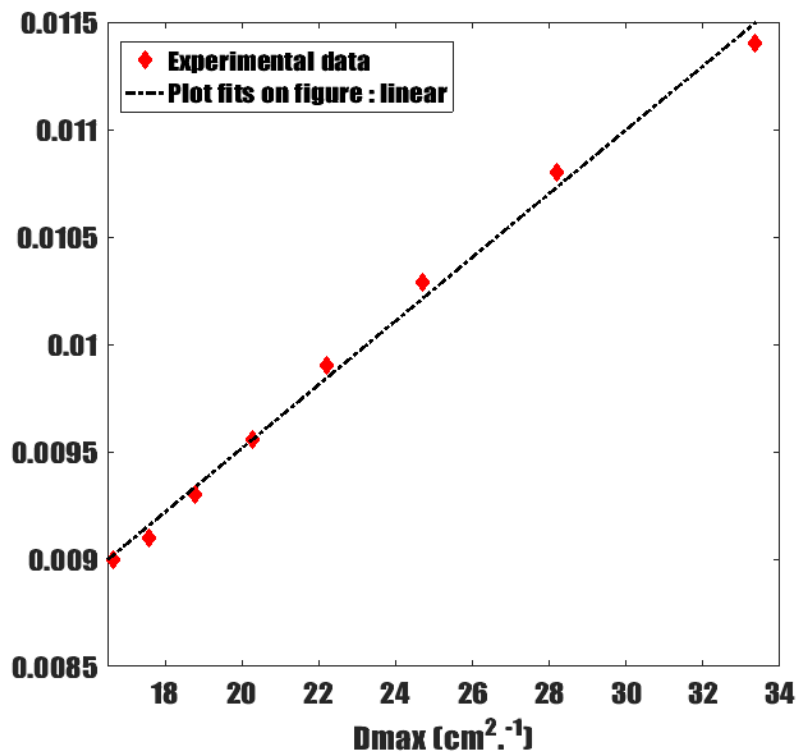


Figure 4: Optimum thickness versus D_{max}



Figure .4 shows an increasing linear function of the optimum thickness of the base with the maximum of the diffusion coefficient, expressed by equation 18 as:

$$Hopt(cm) = 1.5 \cdot 10^{-4} \times Dmax + 0.0066 \tag{18}$$

Figures. 5 and 6, respectively have a decreasing function of the optimum thickness with both, the temperature and the applied magnetic field.

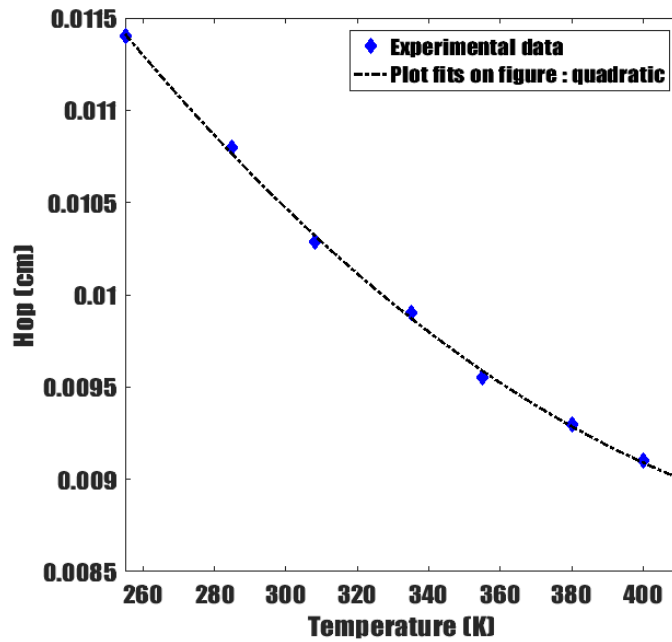


Figure 5: Optimum thickness versus temperature

Equation 19, below, represents the fit of the curve in Figure 5.

$$Hopt(cm) = 5 \cdot 10^{-8} \times T^2 - 4.8 \cdot 10^{-5} \times T(K) + 0.021 \tag{19}$$

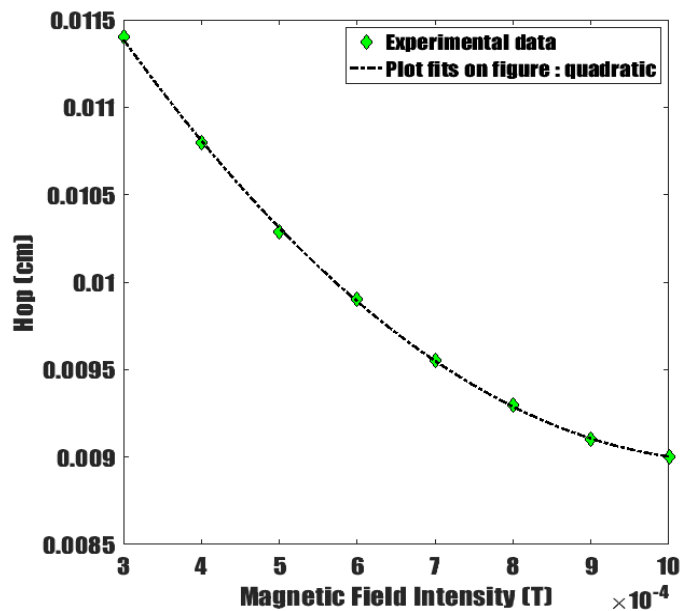


Figure 6: Optimum thickness versus magnetic field

Equation 20 represents the fit of the curve in **Figure 6**.

$$H_{opt}(cm) = 4 \cdot 10^3 \times B^2 - 8.6 \times B(T) + 0.014 \quad (20)$$

The short-circuit current density, corresponding to the large values of the recombination velocity at the junction, decreases as a function of the maximum diffusion coefficient (**Figure 2**), which itself decreases with the optimum temperature and the applied magnetic field (**Table .1**). The diffusion length of minority carriers (**Eq. 5**), consequently, decreases with the maximum diffusion coefficient, when the optimum temperature and the applied magnetic field increase. Thermal agitation and deflection, then impose, a short distance of course to the minority carriers, photogenerated from the rear face, in depth towards the junction (low $\alpha(\lambda)$)[31, 69]. The results from the table. 1, confirms the need to produce thin bifacial solar cells [12, 13,74, 75, 76], to improve significant efficiency.

4. Conclusion

This work has pointed out a graphical technique for determining the optimum base thickness of bifacial silicon solar cell back illuminated with monochromatic light of weak absorption coefficient.

Indeed excess minority carriers' maximum diffusion coefficient obtained as mathematical co-relationships with optimum temperature point for given magnetic field, is used. The magneto-transport equation relating to the density of the minority carriers in the base of bifacial solar cell was solved. Boundary conditions, were taken into account through recombination velocity in front and rear face.

Study from the photocurrent density has produced expressions of minority carriers' recombination velocity on the back side. Graphical technique is used to analyze back surface recombination velocity expressions versus thickness, and then, optimum thickness of the base of the silicon bifacial solar cell was deduced and fitted as decreasing functions of both, the temperature and the magnetic field.

References

- [1]. Yadav, P., Pandey, K., Tripathi, B., Kumar, C.M., Srivastava, S.K., Singh, P.K. and Kumar, M. (2015) An Effective Way to Analyze the Performance Limiting Parameters of a Poly-Crystalline Silicon Solar Cell Fabricated in the Production Line. *Solar Energy*, 122, 1-10. <https://doi.org/10.1016/j.solener.2015.08.005>
- [2]. X. Sun, M. R. Khan, C. Deline and M. A. Alam (2018). Optimization and performance of bifacial solar modules: A global perspective. *Appl. Energy*, vol. 212, pp. 1601-1610, <https://doi.org/10.1016/j.apenergy.2017.12.041> .
- [3]. Fossum, J.G. (1977). Physical Operation of Back-Surface-Field Silicon Solar Cells. *IEEE Transactions on Electron Devices*, 2, 322-325. <https://doi.org/10.1109/T-ED.1977.18735>
- [4]. A.Cuevas, R.A. Sinton and R.R.King, A Technology-Based Comparison between Two-Sided and Back-Contact Silicon Solar Cells. The 10th European Photovoltaic Solar Energy Conference, Lisbon, 1991, 8-12, 23-26. https://doi.org/10.1007/978-94-011-3622-8_6
- [5]. T. Uematsu, K. Tsutsui, Y. Yazawa, T. Warabisako, I. I. Araki, Yeguchi and T. Joge (2003). Development of bifacial PV modules for new applications of flat-plate modules. *Solar Energy Materials and Solar cells*, 75, Pp. 557-566.
- [6]. D.L.Meier, J.M. Hwang and R.B.Campbell (1988). The Effect of Doping Density and Injection Level on Minority Carrier Lifetime as Applied to Bifacial Dendritic Web Silicon Solar Cells. *IEEE Transactions on Electron Devices*,, 35, 70-79. <https://doi.org/10.1109/16.2417>
- [7]. A, Aberle, A.G. and R. Hezel, 20% Efficient Bifacial Silicon Solar Cells. 14th European Photovoltaic Solar Energy Conference, Munich, 1997,pp. 92-95.



- [8]. N.Bordin, L. Kreinin and N. Eisenberg, Determination of Recombination Parameters of Bifacial Silicon Cells with a Two Layer Step-Liked Effect Distribution in the Base Region. Proceedings of the 17th European PVSEC, Munich, 22-26 October 2001, 1495-1498.
- [9]. G. Sissoko, E. Nanema, A. Correa, M. Adj, A.L. Ndiaye, M.N. Diarra (1998). Recombination parameters measurement in double sided surface field solar cell. Proceedings of World Renewable Energy Conference, Florence–Italy, pp. 1856–1859
- [10]. A.Gover and P. Stella (1974). Vertical Multijunction Solar-Cell One-Dimensional Analysis. IEEE Transactions on Electron Devices, 21, 351-356.[https://doi.org/ 10.1109/T-ED.1974.17927](https://doi.org/10.1109/T-ED.1974.17927)
- [11]. J.F.Wise,(1970).Vertical Junction Hardened Solar Cell. US Patent, 3, 690-953.
- [12]. Yasar S., Kahraman S., Cetinkaya S., Apaydin S., Bilican I., Uluer I.(2016). Numerical thickness optimization study of CIGS based solar cells with wxAMPS, *Optik*, 127 (20), pp. 8827-8835.
- [13]. Ayed Al Sayem, Yeasir Arafat, Md. Mushfiqur Rahman (2014) Thickness optimization and composition grading effect in heterojunction CIGS Solar Cell. Conference Paper published Dec in 8th International Conference on Electrical and Computer Engineering.
<http://dx.doi.org/10.1109/icece.2014.7026952>
- [14]. R. R. Vardanyan, U. Kerst, B. Tierock, H. G. Wagemann (1997). Measurement of recombination parameters of solar cell in a magnetic field. Proceeding of the 14th European Photovoltaic Solar Energy Conference (Barcelona, Spain). Pp 2367-2369.
- [15]. S.Gupta, P. Ahmed and S.Garg, . A Method for the Determination of the Material parameters D, L, S and α from Measured Short-Circuit Photocurrent. Solar Cells, 1988,25, 61-72. [https://doi.org/10.1016/0379-6787\(88\)90058-0P](https://doi.org/10.1016/0379-6787(88)90058-0P)
- [16]. Dhariwal, S.R. and Vasu, N.K. (1981). A Generalized Approach to Lifetime Measurement in pn Junction Solar Cells. Solid-State Electronics, 24, 915-927. [https://doi.org/10.1016/0038-1101\(81\)90112-X](https://doi.org/10.1016/0038-1101(81)90112-X)
- [17]. Muzeyyen Saritas and Harry D. Mckell (1988). Comparison of minority carrier diffusion length measurements in silicon by the photoconductive decay and surface photovoltage methods. J. Appl.]63 (9) pp. 4561-67
- [18]. Jain, G.C., Singh, S.N. and Kotnala, R.K. (1983). Diffusion Length Determination in n⁺-p⁺-p⁺ Based Silicon Solar Cells from the Intensity Dependence of the Short Circuit for Illumination from the p⁺ Side. Solar Cells, 82, pp.39-48. [https://doi.org/10.1016/0379-6787\(83\)90063-7](https://doi.org/10.1016/0379-6787(83)90063-7)
- [19]. Sissoko, G., Museruka, C., Corréa, A., Gaye, I. and Ndiaye, A.L. (1996). Light Spectral Effect on Recombination Parameters of Silicon Solar Cell. World Renewable Energy Congress, Pergamon, Part III, pp.1487-1490.
- [20]. O. Diasse, A. Diao, I. Ly, M.S. Diouf, I. Diatta, R. Mane, Y. Traore and G.Sissoko (2018). Back Surface Recombination Velocity Modeling in White Biased Silicon Solar Cell under Steady State. Journal of Modern Physics, 9, 189-201. <https://doi.org/10.4236/jmp.2018.92012>
- [21]. H.L.Diallo, A.S. Maiga, A. Wereme and G. Sissoko, (2008). New Approach of both Junction and Back Surface Recombination Velocities in a 3D Modelling Study of a Polycrystalline Silicon Solar Cell. The European Physical Journal Applied Physics, 42, 193-211. <http://dx.doi.org/10.1051/epjap:2008085>
- [22]. E.Gaubas and J. Vanhellemont (1996). A simple Technique for the Separation of Bulk and Surface Recombination Parameters in Silicon. Journal of Applied Physics, 80, 6293-6297. <https://doi.org/10.1063/1.363705M>
- [23]. Demesmaeker, E., Symons, J., Nijs, J. and Mertens, R. (1991). The Influence of Surface Recombination on the Limiting Efficiency and Optimum Thickness of Silicon Solar Cells. 10th European Photovoltaic Solar Energy Conference, Lisbon, 8-12 April 1991, 66-67. https://doi.org/10.1007/978-94-011-3622-8_17



- [24]. K. Misiakos, C. H. Wang, A. Neugroschel and F. A. Lindholm (1990). Simultaneous extraction of minority carrier parameters in crystalline semiconductors by lateral photocurrent. *J. Appl. Phys.* 67(1): 321-333.
- [25]. K. Bouzidi, M. Chegaar, A. Bouhemadou (2007). Solar cells parameters evaluation considering the series and shunt resistance. *Solar Energy Materials & Solar Cells*. Volume 91, Issue 18, 6, Pp. 1647-165. <https://doi.org/10.1016/j.solmat.2007.05.019>
- [26]. M. Bashahu and A. Habyarimana (1995). Review and test of methods for determination of the solar cell series resistance. *Renewable Energy*, 6, 2, pp. 127-138, [https://doi.org/10.1016/0960-1481\(94\)E0021-V](https://doi.org/10.1016/0960-1481(94)E0021-V)
- [27]. El-Adawi, M.K. and Al-Nuaim, I.A. (2002). A Method to Determine the Solar Cell Series Resistances from a Single I-V Characteristic Curve Considering Its Shunt Resistance—New Approach. *Vacuum*, 64, 33-36. [http://dx.doi.org/10.1016/S0042-207X\(01\)00370-0](http://dx.doi.org/10.1016/S0042-207X(01)00370-0)
- [28]. Diatta, I. Ly, M. Wade, M. S. Diouf, S. Mbodji, G. Sissoko, (2017) Temperature Effect on Capacitance of a Silicon Solar Cell under Constant White Biased Light. *World Journal of Condensed Matter Physics*, 6, pp.261-268.
- [29]. El-Basit, W.A., Abd El-Maksood, A.M. and El-Moniem Saad Soliman, F.A. (2013) Mathematical Model for Photovoltaic Cells. *Leonardo Journal of Sciences*, 23, 13-28. <http://ljs.academicdirect.org>
- [30]. Lovejoy, M.L., Melloch, M.R., Ahrenkiel, R.K. and Lundstrom, M.S. (1992) Measurement Considerations for Zero-Field Time-of-Flight Studies of Minority Carrier Diffusion in III-V Semiconductors. *Solid-State Electronics*, 35, 251-259. [https://doi.org/10.1016/0038-1101\(92\)90229-6](https://doi.org/10.1016/0038-1101(92)90229-6)
- [31]. M. Kunst, G. Muller, R. Schmidt and H. Wetzel (1988) Surface and volume decay processes in semiconductors studied by contactless transient photoconductivity measurements. *Appl. Phys.*, Vol. 46, (1988), pp.77-85.
- [32]. G.Sissoko, S. Sivoththanam, M. Rodo and P. Mialhe, Constant Illumination-Induced Open Circuit Voltage Decay (CIOCVD) Method, as Applied to High Efficiency Si Solar Cells for Bulk and Back Surface Characterization. 11th European Photovoltaic Solar Energy Conference and Exhibition, Montreux, 12-16 October 1992, 352-354.
- [33]. Anil Kumar, R., Suresh, M.S. and Nagaraju, J. (2001) Measurement of AC Parameters of Gallium Arsenide (GaAs/Ge) Solar Cell by Impedance Spectroscopy. *IEEE Transaction on Electron Devices*, 48, 2177-2179. <https://doi.org/10.1109/16.944213>
- [34]. Fabrick, L.B. and Eskenas, K.L. (1985) Admittance Spectroscopy and Application to CuInSe₂ Photovoltaic Devices. In *Proc of the IEEE PVSC, Las Vegas, 21-25 October 1985*, 754-757.
- [35]. Mora-Sero, I., Garcia-Belmonte, G., Boix, P.P., Vazquez, M.A. and Bisquert, J. (2009) Impedance Spectroscopy Characterization of Highly Efficient Silicon Solar Cells under Different Illumination Intensities Light. *Energy and Environmental Science*, 2, 678-686. <https://doi.org/10.1039/b812468j>
- [36]. Sahin, G., Dieng, M., Moujtaba, M., Ngom, M., Thiam, A. and Sissoko, G. (2015) Capacitance of Vertical Parallel Junction Silicon Solar Cell under Monochromatic Modulated Illumination. *Journal of Applied Mathematics and Physics*, 3, 1536-1543. <https://doi.org/10.4236/jamp.2015.311178>
- [37]. D. Chenvidhya, K. Kirtikara, C. Jivacate (2003). A new characterization method for solar cell dynamic impedance. *Solar Energy and Solar Cells*. Volume 80, Issue 4, Déc. 2003, Pp. 459-464. <https://doi.org/10.1016/j.solmat.2003.06.011>
- [38]. Diao, A., Thiam, N., Zoungrana, M., Sahin, G., Ndiaye, M. and Sissoko, G. (2014) Diffusion Coefficient in Silicon Solar Cell with Applied Magnetic Field and under Frequency: Electric Equivalent Circuits. *World Journal of Condensed Matter Physics*, 4, 84-92. <https://doi.org/10.4236/wjcmp.2014.42013>



- [39]. Sarfaty, R., Cherkun, A., Pozner, R., Segev, G., Zeierman, E., Flitsanov, Y., Kribus, A. and Rosenwaks, Y. (2011). Vertical Junction Si Micro-Cells for Concentrating Photovoltaics. Proceedings of the 26th European Photovoltaic Solar Energy Conference and Exhibition, Hamburg, 5-6 September 2011, 145-147.
- [40]. Amary Thiam, Gokhan Sahin, Mohamed Abderrahim Ould El Moujtaba , Babacar Mbow, Marcel Sitor Diouf, Moussa Ibra Ngom, Grégoire Sissoko(2015). Incidence angle effect on electrical parameters of a bifacial silicon solar cell illuminated by its rear side in frequency domain. *Int. J. Pure Appl. Sci. Technol.*, Vol. (30), pp. 29-42, www.ijopaasat.in
- [41]. R. Gopal, R. Dwivedi, S. K. Srivastava (1986). Effect of non-uniform illumination on the photovoltaic decay characteristic of solar cells. *IEEE, Trans. Elect. Dev.* Vol. ED-33, no 6, Pp. 802-809.
- [42]. Furlan, J. and Amon, S. (1985) Approximation of the Carrier Generation Rate in Illuminated Silicon. *Solid-State Electronics*, 28, 1241-1243. [https://doi.org/10.1016/0038-1101\(85\)90048-6](https://doi.org/10.1016/0038-1101(85)90048-6).
- [43]. E.D. Stokes and T.L.Chu (1977). Diffusion Lengths in Solar Cells from Short-Circuit Current Measurements. *Applied Physics Letters*, 30, 425-426. <https://doi.org/10.1063/1.89433>
- [44]. Ly, I., Zerbo, I., Wade, M., Ndiaye, M., Dieng, A., Diao, A., Thiam, N., Thiam, A., Dione, M.M., Barro, F.I., Maiga, A.S. and Sissoko, G. (2011). Bifacial Silicon Solar Cell under Frequency Modulation and Monochromatic Illumination: Recombination Velocities and Associated Equivalent Electrical Circuits. Proceedings of 26th European Photovoltaic Solar Energy Conference and Exhibition, Hamburg, 5-9 September 2011, 298-301.I.
- [45]. N. Thiam, A. Diao, M. Ndiaye, A. Dieng, A.Thiam, M. Sarr, A.S. Maiga and G.Sissoko, Electric Equivalent Models of Intrinsic Recombination Velocities of a Bifacial Silicon Solar Cell under Frequency Modulation and Magnetic Field Effect. *Research Journal of Applied Sciences, Engineering and Technology*, 2012,4, 4646-4655.
- [46]. C.H.Wang and A. Neugroschel (1991). Minority-Carrier Lifetime and Surface Recombination Velocity Measurement by Frequency-Domain Photoluminescence. *IEEE Transactions on Electron Devices*,38, 2169-2180. <https://doi.org/10.1109/16.83745>
- [47]. Wafaa Abd El-Basit, Ashraf Mosleh Abd El-Maksood and Fouad Abd El-Moniem Saad Soliman (2013). Mathematical Model for Photovoltaic Cells. *Leonardo Journal of Sciences*, Issue 23, pp.13-28. (<http://ljs.academicdirect.org/>)
- [48]. P. Singh, S.N. Singh, M. Lal, M. Husain (2008). Temperature dependence of I–V characteristics and performance parameters of silicon solar cell. , *Solar Energy Materials & Solar Cells*, 92, pp.1611–1616.
- [49]. Dorkel, J.M. and Leturcq, P. (1981) Carrier Mobilities in Silicon Solar Semi-Empirically Related Temperature, Doping and Injection Level. *Solid State Electron*, 24, 821-825. [https://doi.org/10.1016/0038-1101\(81\)90097-6](https://doi.org/10.1016/0038-1101(81)90097-6)
- [50]. Betsler, Y., Ritter, D., Bahir, G., Cohen, S. and Serling, J. (1995). Measurement of the Minority Carrier Mobility in the Base of Heterojunction Bipolar Transistors Using a Magneto Transport Method. *Applied Physics Letters*, 67, 1883-1884. <https://doi.org/10.1063/1.114364>
- [51]. Flohr, Th. and Helbig, R. (1989). Determination of Minority-Carrier Lifetime and Surface Recombination Velocity by Optical-Beam-Induced-Current Measurements at Different Light Wavelengths. *Journal of Applied Physics*, 66, 3060-3065. <https://doi.org/10.1063/1.344161>
- [52]. F. Toure, M. Zougrana, B. Zouma, S. Mbodji, S. Gueye, A. Diao & G. Sissoko (2012). Influence of Magnetic Field on Electrical Model and Electrical Parameters of a Solar Cell Under Intense Multispectral Illumination. *Global Journal of Science Frontier Research (A)* Vol. XII, issue VI, Version I, pp 51-59.



- [53]. M. Zoungrana, B. Dieng, O.H. Lemrabott, F. Toure, M.A. Ould El Moujtaba, M.L. Sow And G. Sissoko (2012). External Electric Field Influence on Charge Carriers and Electrical Parameters of Polycrystalline Silicon Solar Cell. *Research Journal of Applied Sciences, Engineering and Technology* 4(17); 2967-2972. 2012.
- [54]. M.L.Ba, N. Thiam, M. Thiame, Y. Traore, M.S. Diop, M. Ba, C.T. Sarr, M. Wade and G.Sissoko, Base Thickness Optimization of a (n⁺-p-p⁺) Silicon Solar Cell in Static Mode under Irradiation of Charged Particles. *Journal of Electromagnetic Analysis and Applications*, 2019, 11, 173-185. <https://doi.org/10.4236/jemaa.2019.1110012>
- [55]. Amadou Sarr Gning, Mamadou Lamine Ba, Mamour Amadou Ba, Gora Diop, Ibrahima Diatta, El Hadji Sow, Oulimata Mballo and Gregoire Sissoko, Optimum base thickness determination of a back illuminated silicon solar cell: irradiation effect. *International Journal of Advanced Research*, 2020, 8(07), 100-109. <http://dx.doi.org/10-21474/IJAR01/11268>
- [56]. Mor Sarr, Idrissa Gaye, Seydi Ababacar Ndiaye, Mamadou Lamine Ba, Gora Diop, Ibrahima Diatta, Lemrabott Habiboullah, Gregoire Sissoko (2021). Effet de l'irradiation par des particules chargees sur le coefficient de diffusion de la base d'une photopile au silicium (n⁺-p-p⁺) : determination de l'epaisseur optimum sous eclairage monochromatique. *International Journal of Advanced Research*. 9(03), 127-135. <http://dx.doi.org/10.21474/IJAR01/12565>
- [57]. Sega Diagne, Ousmane Sow, Gora Diop, Richard Mane, Ibrahima Diatta, Djiby Ndongue, Youssou Traore, Lemrabott Habiboullah, Mamadou Wade and Gregoire Sissoko. (2022) Optimization of silicon solar cell base thickness, while illuminated by a long wavelength monochromatic light: influence of both Lorentz law and Umclapp process. *International Journal of Advanced Research*, 10(08), 133-143. <http://dx.doi.org/10.21474/IJAR01/151508>
- [58]. Malick Ndiaye, Ousmane Sow, IbrahimaDiatta, Gora Diop, Dibor Faye, KhadyLoum, YoussouTraore, MoustaphaThiame, Mamadou Wade And GregoireSissoko (2022). Optimization of the thickness of the doping rate base (Nb) of the (n⁺/p/p⁺) silicon solar cell with vertical multi-junction connected in series and placed under monochromatic illumination in frequency modulation. *Journal of Chemical, Biological and Physical Sciences*, Vol. 12, N^o 4, 266-280. <https://doi.org/10.24214/jebps.C.12.4.26680>
- [59]. Richard, M., Ibrahima, L., Mamadou, W., Ibrahima, D., Marcel, S.D., Youssou, T., Mor, N., Seni, T. and Grégoire, S. (2017) Minority Carrier Diffusion Coefficient D*(B, T): Study in Temperature on a Silicon Solar Cell under Magnetic Field. *Energy and Power Engineering*, 9, 1-10. <http://www.scirp.org/journal/epehttps://doi.org/10.4236/epe.2017.91001>
- [60]. Seydina, D., Mor, N., Ndeye, T., Youssou, T., Mamadou, L.B., Ibrahima, D., Marcel, S.D., Oulimata, M., Amary, T. and Grégoire, S. (2019) Influence of Temperature and Frequency on Minority Carrier Diffusion Coefficient in a Silicon Solar Cell Under Magnetic Field. *Energy and Power Engineering*, 11, 355-361. <https://doi.org/10.4236/epe.2019.1110023>
- [61]. A. Ndiaye, S. Gueye, M. Mbaye Fall, G. Diop, A. Ba, M. Ba, I. Diatta, L. Habiboullah and G.Sissoko, Diffusion Coefficient at Resonance Frequency as Applied to n⁺/p/p⁺ Silicon Solar Cell Optimum Base Thickness Determination. *Journal of Electromagnetic Analysis and Applications*, 2020,12, 145-158. doi: 10.4236/jemaa.2020.1210012.
- [62]. Dieng, A., Zerbo, I., Wade, M., Maiga, A.S. and Sissoko, G. (2011). Three-Dimensional Study of a Polycrystalline Silicon Solar Cell: The Influence of the Applied Magnetic Field on the Electrical Parameters. *Semiconductor Science and Technology*, 26, Article ID: 095023. <http://dx.doi.org/10.1088/0268-1242/26/9/095023>
- [63]. E. Sow, S. Mbodji, B. Zouma, M. Zoungrana, I. Zerbo, A. Sere & G. Sissoko (2012). Using Gauss Law in determining the width emitter extension region of the solar cell operating in open circuit



- condition. Global Journal of Science Frontier Research Physics and Space Sciences Volume 12 Issue 6 Version 1.0, p67-72, Year 2012. Online ISSN: 2249-4626 & Print ISSN: 0975-5896
- [64]. Chen H. R, Lee. C. P, Chang. C. Y, Tsang, J. S, Tsai. K. L (2009). The study of emitter thickness effect on the heterostructure emitter bipolar transistors. *Journal of Applied Physics*, 74 (2), 1398-1402.
- [65]. M. Dieng, B. Seibou, I. Ly, M. Sitor Diouf, M. Wade and G. Sissoko, Silicon Solar Cell Emitter Extended Space Charge Region Determination under Modulated Monochromatic Illumination by using Gauss's Law. *International Journal of Innovative Technology and Exploring Engineering*, 2017, 6, 17-20
- [66]. Sega Diagne, Gora Diop, Richard Mane, Malick Ndiaye, Ibrahima Diatta, Gilbert N Dione, Ousmane Sow, Moustapha Thiame, Mamadou Wade and Gregoire Sissoko (2020). Monochromatic light of short wavelength as applied to determine (n+/p/p+) silicon solar cell base thickness under the influence of both magnetic field and temperature. *International Journal of Engineering Research Updates*, 2022, 03(02), 013–025. DOI: <https://doi.org/10.53430/ijeru.2022.3.2.0055>
- [67]. Ousmane Sow, Sega Gueye, Richard Mane, Gora Diop, Ibrahima Diatta, Khady Loum, Moustapha Thiame, Mamadou Wade and Gregoire Sissoko. (2022). (n+/p/p+) silicon solar cell base thickness optimization under modulated short wavelength illumination, at resonances in both frequency and temperature of minority carriers Diffusion coefficient. *International Journal of Engineering Research Updates*, 03(02), 040–052. DOI url: <https://doi.org/10.53430/ijeru.2022.3.2.0059>
- [68]. K.Rajkanan, R. Singh and J. Schewchun (1972). Absorption coefficient of silicon for solar cell calculations. *Solid-State Electronics*, 22,793-795. [https://doi.org/10.1016/0038-1101\(79\)90128-X](https://doi.org/10.1016/0038-1101(79)90128-X)
- [69]. U.C.Ray and S.K.Agarwal, Wavelength (1988). Dependence of Short-Circuit Current Decay in Solar Cells. *Journal of Applied Physics*, 63, 547-549. <https://doi.org/10.1063/1.340084>
- [70]. Ly, I., Ndiaye, M., Wade, M., Thiam, N., Sega, Gueye. And Sissoko, G. (2013) Sissoko Concept of Recombination Velocity S_{fc} at the Junction of a Bifacial Silicon Solar Cell, in Steady State, Initiating the Short-Circuit Condition. *Research Journal of Applied Sciences, Engineering and Technology*, 5, 203-208. <https://doi.org/10.19026/rjaset.5.5105>
- [71]. O. Diasse, R. S. Sam, H. L. Diallo, M. Ndiaye, N. Thiam, S. Mbodji and G. Sissoko (2012). Solar cell's classification by the determination of the specific values of the back surface recombination velocities in open circuit and short-circuit operating conditions. *International Journal of Emerging Trends & Technology in Computer Science (IJETCS)*, 2012, 2278/6856: (pp.18-23)
- [72]. Dede, M.M.S., Ba, M.L., Ba, M.A., Ndiaye, M., Gueye, S., Sow, E. H., Diatta, I., Diop, M.S., Wade, M. and Sissoko, G. (2020) Back Surface Recombination Velocity Dependent of Absorption Coefficient as Applied to Determine Base Optimum Thickness of an n+/p/p+ Silicon Solar Cell. *Energy and Power Engineering*, 12, 445-458. <https://doi.org/10.4236/epe.2020.127027>
- [73]. Maimouna Mint ELY, Ndeye Thiam, Mor Ndiaye, Youssou Traore, Richard Mane, El hadji Sow, Oulimata mballo, Masse Samba Dieng, Cheikh Tidiane Sarr, Ibrahima Ly, Gregoire Sissoko, (2020) Surface recombination velocity concept as applied to determinate back surface illuminated silicon solar cell base optimum thickness, under temperature and external magnetic field effects. *Journal of Scientific and Engineering Research*, 7(2):69-77, <https://jsaer.com/archive/volume-7-issue-2-2020/>
- [74]. Nobuyuki Andoh, Kenichi Hayashi, Takatoshi Shirasawa, Toshiyuki Sameshima, Koichi Kamisako (2001). Effect of film thickness on electrical property of microcrystalline silicon. *Solar Energy Materials and Solar Cells*, Vol. 66 issue 1-4 Pp. 437-441 [http://dx.doi.org/10.1016/s0927-0248\(00\)00205-1](http://dx.doi.org/10.1016/s0927-0248(00)00205-1)
- [75]. Chung F; Chung-Feng Jeffery Kuo, Hung-Min Tu, Shin-Wei Liang, Wei-Lun Tsai (2010). Optimization of microcrystalline silicon thin film solar cell isolation processing parameters using



- ultraviolet laser. *Optics & Laser Technology*, Vol. 42 issue 6, Pp. 945-955. <http://dx.doi.org/10.1016/j.optlastec.2010.01.013>
- [76]. D. J. Paez, E. Huante-Ceron, A. P. Knights (2013). A Vertical PN Junction Utilizing the Impurity Photovoltaic Effect for the Enhancement of Ultra-thin Film Silicon Solar Cells MRS Proceedings Vol. 1536, Pp.39 to 44 <http://dx.doi.org/10.1557/opl.2013.750>

