



Minority Carriers' Diffusion Length Determination in the Base of a Silicon Vertical Junction Solarcell by Use of the Short-Circuit Current Calibration Curve Technique

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Abstract The L_{eff} determination technique is applied to the lamella base of parallel vertical junction silicon solar cell under steady state. The theoretical current density's expression generated by the lamellasolar cell under polychromatic illumination is established. The short-circuit current's calibration curve compared to the experimental one yields the minority carriers effective diffusion length. The purpose of this paper is to improve curves calibration technique by proposing a method based on an algorithm called "*Find L_{eff}* ".

Keywords Vertical silicon solar cell- Diffusion length- Algorithm

Introduction

In order to improve the photovoltaic conversion's efficiency, solar cells, in particular silicon solar cells, have undergone architectural modifications. Consisting by an emitter-base junction (n/p), the illumination is provided by the front surface (monofacial), which constitutes the emitter. As a result, the structure has become (n⁺-p-p⁺), improving the quality of both the emitter and the base. At the back of the base (p-p⁺) where an electric field is produced using the (p⁺) layer, which returns the electric charges to the junction [1-5]. Illumination may be performed either from the front (n⁺) and from the rear (p⁺) or simultaneously from both sides (bifacial or double side surface field solar cells) [6-8].

The lateral (or parallel) illumination of junction (space charge region) plane of (n/p) or (n⁺/p/p⁺) has led to the realization of new architectures, which are the vertical junction (VJ) solar cells [9-10]. The vertical junction gives the advantage of uniform photo-creation of electric charges near (n/p) or (p/p⁺) surfaces, in order to promote their collection and to contribute to the photocurrent. Thus the unit structures (n/p) and (n⁺/p/p⁺) can be reproduced and connected to give multiple vertical junction solar cells (MVJs) [11-13]. These (MVJs) lead to two connection possibilities. These are serial MVJs and parallel MVJs. Serial MVJs mainly use (n⁺/p/p⁺) connected in series to increase the output electrical voltage [14], whereas parallel MVJs use (n/p) structures which are connected to each other in parallel, i.e. the bases connected to each other and the emitters connected to each other, in order to increase the output electrical current, from the contribution of the different areas of the structure [11-12, 15].

These structures allow the creation of electrical charges close to the surfaces (n/p) and (p/p⁺), and give the advantage of choosing poor quality silicon base materials with low optoelectronic properties (weak lifetime and diffusion length) and also can be submitted to concentration of incident light (number of suns) [16-17].

Thus this work brings the interest of minority charge carriers' diffusion length determination in the base(p) of parallel vertical junction solar cell. The intercept technique of the calibration curve of the theoretical



photocurrent with the experimental short-circuit current, represented as a function of minority carriers' diffusion length, is improved by the new method (Leff find).

Theoretical Study

Figure 1 shows a parallel vertical junction silicon solar cell under polychromatic illumination.

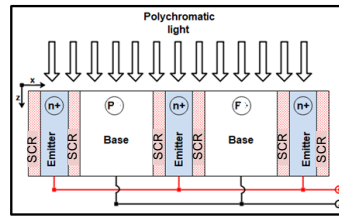


Figure 1: Solar cell with vertical junction connected in parallel

Diffusion Continuity Equation

When the solar cell is illuminated, there are the establishment of phenomena's such as, absorption- generation, diffusion and recombination of excess minority carriers charges $\delta(x, z)$ at the abscissa x and the depth z in the base. In steady state, these phenomena are taken into account through the continuity equation given by following relation [11, 18]:

$$\frac{\partial^2 \delta(x)}{\partial x^2} - \left(\frac{1}{L^2}\right) \cdot \delta(x) = -\frac{G(z)}{D} \quad (1)$$

L and D , represent respectively the diffusion length and coefficient of minority carriers in the base and linked by Einstein's relationship:

$$L^2 = D\tau \quad (2)$$

$G(z)$ denotes the minority carrier generation rate, at depth z in the base, while the solar cell is illuminated with polychromatic light. Its expression is given by:

$$G(Z) = n \sum_{i=1}^3 a_i e^{-b_i Z} \quad (3)$$

Where the coefficients a_i and b_i , represent the tabulated values under the solar light spectrum, corresponding to $n=1$ sun [19, 20]. The sun irradiation concentration is represented by n [15-17, 21]

The general solution's expression of differential equation with second member is given by following relation:

$$\delta(x, z, Sf, n) = A(z, Sf, n) \cdot \cosh\left(\frac{x}{L}\right) + B(z, Sf, n) \cdot \sinh\left(\frac{x}{L}\right) + \sum_{i=1}^3 K(n) \cdot e^{-b_i z} \quad (4)$$

Where $K(n) = \frac{n \cdot a_i \cdot L^2}{D[1 - (L \cdot b_i)^2]}$, A and B are determined using the following boundary conditions:

Boundary Conditions

At junction in $x = 0$:

$$D_n \cdot \frac{\partial}{\partial x} \delta(x, z) \Big|_{x=0} = S_f \cdot \delta(0, z) \quad (5)$$

S_f , represents the excess minority carrier recombination velocity at the junction, and characterizes charge current flow through the junction surface [22-24]. It indicates also the solar cell operating point through the variation of the gradient at the junction, from ideal open circuit ($S_f = 0$) to short circuit condition i.e. large S_f values. In real open circuit condition an additional component (S_f0) is taken into account, associated to losses through shunt resistance [25-28].

At base middle, at $x = H/2$, base can be split in two, to get two $H/2$ base solar cells, with two adjacent emitters (Figure 2). Then each half appears to be an ideal back surface field solar cell, with zero back surface recombination velocity ($S_b = 0$) [11-12, 18, 28-32]:



$$\left. \frac{\partial}{\partial x} \delta(x, z) \right|_{x=\frac{H}{2}} = 0 \quad (6)$$

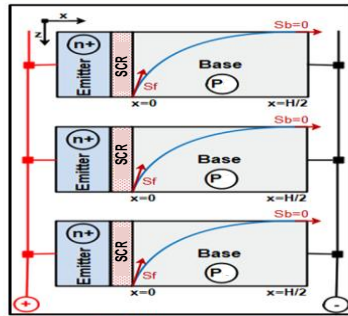


Figure 2: Solar cell with vertical junction connected in parallel

Photocurrent density and short-circuit photocurrent density

Fick's Law, allows us to establish photocurrent density equation due to charge carrier's diffusion through the junctions that frame base [11].

$$J_{ph} = 2 \cdot q \cdot D_n \cdot \left. \frac{\partial}{\partial x} \delta(x, z) \right|_{x=0} \quad (7)$$

Figure 3 shows photocurrent and short circuit photocurrent densities' profiles versus junction recombination velocity.

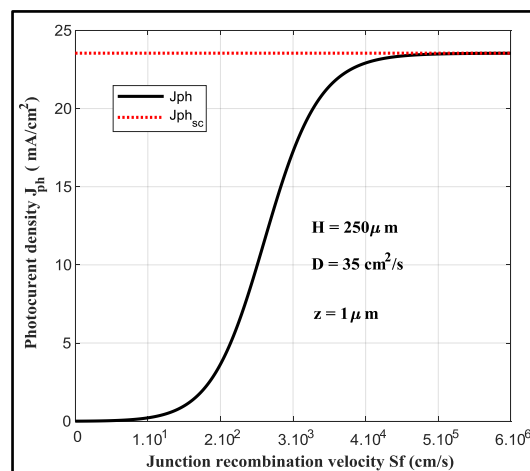


Figure 3: Photocurrent and short-circuit photocurrent versus Sf

Short-circuit photocurrent density

Near very high junction recombination velocity's values, photocurrent density (Jph) tends towards a constant value which corresponds to the short-circuit current (Jph_{sc}).

$$J_{sc} = \lim_{S_f \rightarrow \text{high value}} J_{ph} \quad (8)$$

Figure 4 shows short-circuit current's profile versus diffusion length.



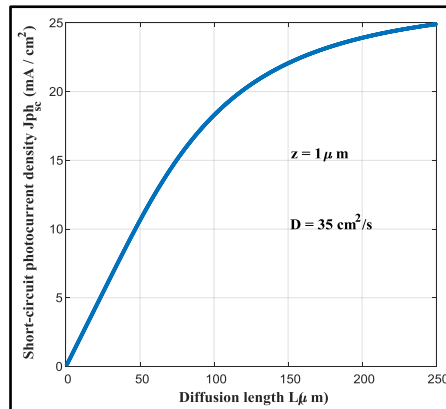


Figure 4: Variation of short-circuit current ($J_{ph_{SC}}$) versus diffusion length

Effective diffusion length L_{eff} measurement

Determination method of L_{eff} value

The short-circuit current calibration curve technique

This method is based on intersection point of theoretical short-circuit current density curve with experimental curve [12, 25, 33]. The orthogonal projection intercept point of theoretical and experimental curves on diffusion length axis corresponds to L_{eff} value.

New determination method based on an algorithm

The freehand projection on short-circuit photocurrent density curve to determine L_{eff} value probably induces errors, and considerably influences the interpreted results. The new method proposed in this paper consists to calculate effective diffusion length value by using an algorithm called " $Find_{L_{eff}}$ " described by Figure 5.

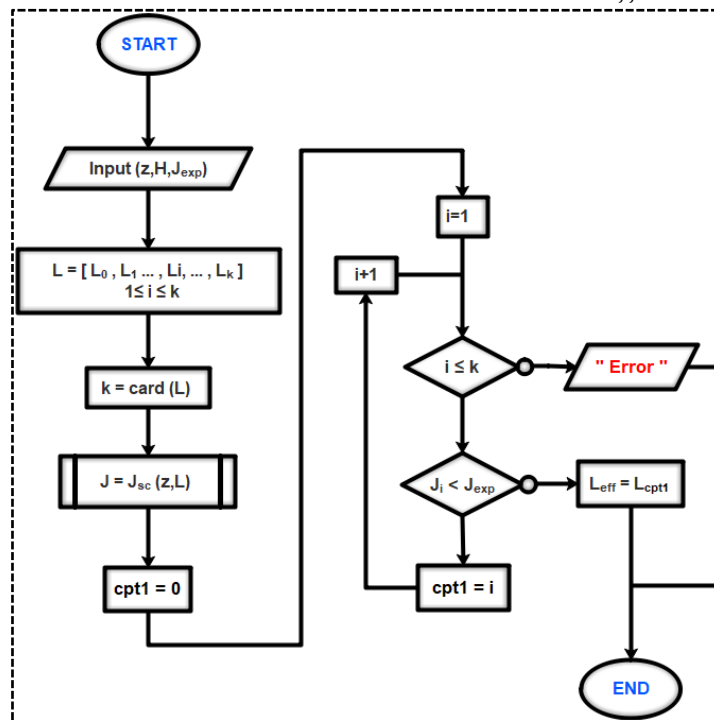


Figure 5: L_{eff} calculation method flowchart

The new L_{eff} calculating method using in this paper consists: firstly, discretizing the solar cell base width value, then determining corresponding photocurrent values. Thus a short-circuit photocurrent density vector evolving as a function of the solar cell base width is generated by the algorithm.

$$\left. \begin{aligned} J &= J_{sc}(z, L), \\ L &= [L_1, \dots, L_j, \dots, L_q] \text{ and } 1 \leq i \leq k \end{aligned} \right\} \Leftrightarrow J = [J_1, \dots, J_i, \dots, J_k] \quad (9)$$

The final step corresponds to curves calibration by defining a counting variable which will make it possible to enumerate comparison of the short-circuit photocurrent density with respect to a known experimental value, as the comparison process progresses, the counter variable is incremented at same rate. At end, algorithm returns the "ith" J_{sc} value which respects to the condition:

$$J_i \leq J_{exp} \quad (10)$$

The effective diffusion length is "ith" element's value of vector L. Figure 6 shows L_{eff} graphical determination for different experimental photocurrent (J_{exp}) values obtained in [34] using the algorithm "Find_Leff" [12, 25, 33].

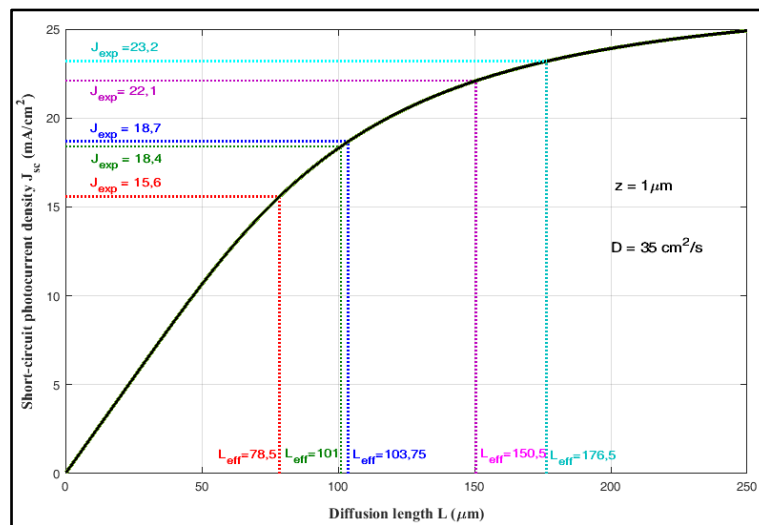


Figure 6: Graphical determination of L_{eff} for different specific J_{exp} values

The results shown in Figure 6 allow us to draw up the following table of correspondence:

Table 1: L_{eff} values obtained from our algorithm with different experimental short-circuit currents

Samples	Experimental J_{SC} (mA) [34]	L_{eff} (µm)
A	15.6	78.50
B	18.4	101
C	18.7	103.75
D	22.1	150.5
E	23.2	176.5

The application of this new algorithm is a great contribution in the precision in the results obtained in the determination of L_{eff} from samples prepared under different elaboration processes [34], having produced these short-circuit current. The L_{eff} obtained is in good agreement with the lamella silicon solar cells processing.

Based on this innovation brought by the Leff finder algorithm, further investigations will be carried out on lamella, using models that take into account the real excess minority carriers effective recombination velocity Sb [35-36].

Conclusion

In this paper, we investigated the determination of the diffusion length of minority carriers in the base of a silicon-parallel vertical junction solar cell using the short-circuit current calibration curve technique. This study highlights diffusion length importance on solar cell manufacturing.

New method proposed in this paper allows an automatically L_{eff} determination by using an algorithm, which considerably reduces the errors risk compared to classical method. Effective diffusion length's knowledge will permit to determine junction intrinsic recombination velocity's of minority carriers in solar cell. Other way, use

algorithmic method offers possibility of better studying L_{eff} behaviour under the influence of external parameters such as temperature, magnetic field, electric field, and light irradiation intensity.

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