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## Theoretical Comparison of SARIMAX and DeepAR models for Time Series Forecasting

Bhargava Kumar<sup>1</sup>, Tejaswini Kumar<sup>2</sup>

<sup>1</sup>Independent Researcher Columbia University Alumni

<sup>2</sup>Bachelor's in CS Candidate University College Dublin

Email: [bhargava1409@gmail.com](mailto:bhargava1409@gmail.com), [tejaswini1000@gmail.com](mailto:tejaswini1000@gmail.com)

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**Abstract** Time series forecasting is a critical element in several fields, facilitating decision-making through predictive insights. This paper presents a comprehensive theoretical analysis of two widely-recognized techniques: SARIMAX, a deterministic method rooted in statistical modeling, and DeepAR, a probabilistic approach that employs recurrent neural networks. The analysis evaluates the fundamental principles, modeling capabilities, handling of uncertainties, computational aspects, and practical considerations of these methods. SARIMAX is distinguished by its capacity to capture linear dependencies and seasonal patterns, whereas DeepAR excels at modeling intricate non-linear relationships and providing probabilistic forecasts with uncertainty estimates. The comparison focuses on flexibility, scalability, computational efficiency, and suitability for various forecasting scenarios. The findings from this study offer guidance for selecting between SARIMAX and DeepAR based on theoretical considerations, highlighting their respective strengths and implications for advancing time series forecasting methodologies.

**Keywords** Time series forecasting, SARIMAX, DeepAR, Probabilistic forecasting, Neural networks, RNN, LSTM

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### 1. Introduction

Time series forecasting is a vital part of decision-making processes in various sectors, such as economics, finance, healthcare, and environmental science. The process involves predicting future values based on historical data, which allows organizations to anticipate trends, plan resources, and manage risks effectively. Through the years, numerous methodologies have been developed to address the intricate nature of time series data, each with its unique strengths and applications.

Two widely recognized methods for time series forecasting are Seasonal Autoregressive Integrated Moving Average with Exogenous Factors (SARIMAX) [1,2,3] and DeepAR [4,5], a probabilistic forecasting approach based on special type of recurrent neural networks (RNNs) called long short-term memory (LSTM). These methods represent distinct forecasting paradigms: SARIMAX is rooted in traditional statistical modeling, offering deterministic forecasts by capturing linear dependencies and seasonal patterns, whereas DeepAR leverages the power of deep learning to provide probabilistic forecasts, accommodating non-linear relationships and capturing the inherent uncertainties in the data.

The motivation behind this paper is to offer a comprehensive theoretical comparison of SARIMAX and DeepAR. While existing literature often focuses on empirical evaluations, this study emphasizes understanding their foundational principles, modeling capabilities, and practical implications. By examining their theoretical underpinnings, we aim to clarify the strengths, weaknesses, and considerations that guide their application in various forecasting scenarios.



The following text outlines the structure of our study, which consists of several components that are explained in detail below. Section 2 provides a detailed overview of time series forecasting methods, specifically focusing on SARIMAX and DeepAR as representative approaches. Section 3 presents a comparative analysis between SARIMAX and DeepAR, with a particular emphasis on their flexibility, ability to handle uncertainty, scalability, computational efficiency, and practical considerations. Section 4 discusses the implications of the theoretical insights gained in the previous sections and provides guidance on how to choose between SARIMAX and DeepAR based on specific needs. The paper concludes in Section 5 with a summary of the key findings and recommendations for appropriate forecasting methodologies, taking into account the trade-off between interpretability and flexibility in time series forecasting approaches. Finally, Section 6 outlines potential directions for future research and development in time series forecasting methodologies.

The main goal of this study is to advance the understanding and development of time series forecasting techniques and to assist in making informed decisions regarding the selection of the most appropriate methodological approach for different forecasting tasks.

## 2. Theoretical Background

Time series forecasting methods range from traditional statistical approaches to modern machine learning techniques. These methods aim to capture patterns and trends within sequential data to predict future values effectively. SARIMAX and DeepAR are two prominent methods in time series forecasting:

### 2.1 SARIMAX (Seasonal Autoregressive Integrated Moving Average with Exogenous Factors)

SARIMAX [1,2,3] is a classical statistical method widely used for time series forecasting. It combines the autoregressive (AR), moving average (MA), and integrated (I) components to model the time series data. SARIMAX extends the ARIMA model by incorporating seasonal components (SARIMA) to handle seasonal variations in the data. It can also incorporate exogenous variables, which are external factors that may influence the time series, enhancing its predictive capability.

#### Theoretical Foundations of SARIMAX:

- Autoregressive (AR), Moving Average (MA), and Integrated (I) Components: SARIMAX models the data based on past values (AR), past errors (MA), and differencing to achieve stationarity (I).
- Incorporation of Seasonal Factors and Exogenous Variables: SARIMAX extends ARIMA by including seasonal components (SARIMA), allowing it to model and forecast seasonal patterns. Exogenous variables provide additional information that can improve forecasting accuracy.

#### Assumptions and Limitations:

SARIMAX assumes that the data is stationary or can be made stationary through differencing. It assumes linear relationships between variables and may struggle with non-linear patterns. Additionally, SARIMAX can be computationally intensive, especially with large datasets or complex seasonal patterns.

### 2.2 DeepAR (Deep Autoregressive Networks)

DeepAR [4,5] represents a modern approach to time series forecasting, leveraging deep learning techniques, specifically special type of Recurrent Neural Networks (RNNs) called Long Short-Term Memory (LSTM).

#### Theoretical Foundations of DeepAR:

- Recurrent Neural Networks (RNNs) and Long Short-Term Memory (LSTM) networks: DeepAR employs LSTMs, a type of RNN, to model temporal dependencies in time series data by maintaining hidden states that capture information across multiple time steps.
- Probabilistic Forecasting: Rather than providing point estimates, DeepAR generates probabilistic forecasts by predicting the parameters of a chosen probability distribution for future values, thereby allowing it to express uncertainty.
- Training on Multiple Time Series: The model leverages a collection of related time series to learn global patterns, thereby improving forecasting performance, particularly for individual series with limited data.
- Likelihood-based Training: DeepAR maximizes the likelihood of observed data, training the model to produce outputs that best explain the observed time series data given the covariates.



- Incorporation of Covariates: The model can include various covariates, such as time-based features (e.g., day of the week, holidays) and other external variables, which helps to capture seasonality and external influences on the time series.

### 3. Comparative Analysis

#### 3.1 Model Complexity

SARIMA boasts a relatively simple structure compared to DeepAR. Built on well-defined mathematical principles involving autoregressive, integrated, moving average, and seasonal components (ARIMA), it allows for easier interpretation of the factors influencing its predictions. This transparency is a major advantage. However, SARIMA's capability is limited to capturing linear trends and seasonality. When faced with highly non-linear patterns or data with complex interactions between past values, SARIMA might struggle to produce accurate forecasts.

DeepAR takes a different approach, leveraging a complex recurrent neural network (RNN) architecture, specifically LSTMs. RNNs excel at capturing intricate sequential relationships within data. This makes DeepAR significantly more flexible and potentially more powerful for handling non-linear patterns and complex interactions compared to SARIMA. However, this complexity comes at a cost. Due to the nature of RNNs, DeepAR is less interpretable. It's challenging to understand precisely how the model arrives at its predictions, making it a "black box" to some extent.

#### 3.2 Handling of Uncertainty

SARIMAX provides deterministic forecasts, meaning it produces point estimates of future values without explicitly quantifying uncertainty. This approach assumes that historical patterns and relationships captured by the model will continue to hold in the future.

In contrast, DeepAR presents a probabilistic approach to forecasting by modeling the full distribution of potential future outcomes. Utilizing various techniques, such as Gaussian distributions for continuous data, DeepAR provides forecasts along with uncertainty estimates. This approach allows decision-makers to assess the likelihood of different scenarios and make informed decisions under conditions of uncertainty.

#### 3.3 Scalability and Computational Efficiency

SARIMAX is typically scalable for datasets of moderate size and can accommodate various levels of data frequency. Nevertheless, scaling SARIMAX to handle large datasets or high-frequency data may present challenges, especially when multiple exogenous variables or intricate seasonal patterns are involved. As the dataset size increases and the model structure becomes more complex, the computational complexity also rises.

The scalability of DeepAR relies on the hardware resources available for training deep neural networks. The initial training phase can be demanding in terms of computational power and memory. However, once trained, DeepAR can effectively generate forecasts for extensive time series data through its parallel processing capabilities, which are inherent in its neural network architecture.

### 4. Practical Considerations

When deciding between SARIMAX and DeepAR for time series forecasting, several practical considerations come into play, including data requirements, preprocessing steps, model tuning, parameter selection, and interpretability of forecasts and model outputs.

#### 4.1 Data Requirements and Preprocessing

##### SARIMAX:

- Data Requirements: SARIMAX assumes stationary time series data or data that can be made stationary through differencing. It requires historical data that exhibit consistent patterns over time, such as trends and seasonality.
- Preprocessing: Prior to model fitting, preprocessing steps often include checking for stationarity, performing differencing if needed, and identifying and handling missing values. Exogenous variables, if included, must be aligned and cleaned to ensure compatibility with the time series data.



**DeepAR:**

- Data Requirements: DeepAR is a versatile model that can process both stationary and non-stationary time series data, as well as data points with irregular spacing. It exhibits a greater capacity to manage missing values than certain other models. Nevertheless, data normalization and scaling may still be advantageous for effective training, and a substantial proportion of missing values can impede performance.
- Preprocessing: While utilizing DeepAR minimizes the reliance on manual feature engineering, it is still essential to consider data normalization and scaling. Although the model can handle missing data during the training process to some extent, data completeness remains a critical aspect.

**4.2 Model Tuning and Parameter Selection****SARIMAX:**

- Model Tuning: Tuning SARIMAX involves selecting appropriate values for model orders (p, d, q) and seasonal periods (P, D, Q). This process typically requires iterative testing and evaluation based on statistical criteria like AIC (Akaike Information Criterion) or BIC (Bayesian Information Criterion).
- Parameter Selection: Parameters are estimated through techniques such as maximum likelihood estimation (MLE) or state-space methods. Choosing the right combination of parameters is crucial for achieving accurate forecasts and may require domain expertise.

**DeepAR:**

- Model Tuning: The tuning process of DeepAR's model encompasses the selection of hyperparameters that pertain to the network architecture, including the quantity of layers and hidden units in the RNN, specifically the LSTM, the learning rate, and dropout rates, which serve to prevent overfitting.
- Parameter Selection: In addition to the hyperparameters of network architecture, DeepAR necessitates the establishment of parameters connected with the probabilistic forecasting framework, such as the determination of the number of quantiles to predict or the selection of distributional forecasts. Typically, hyperparameter optimization is accomplished through the use of cross-validation and validation sets in order to enhance forecast performance.

**4.3 Interpretability of Forecasts and Model Outputs****SARIMAX:**

- Interpretability: SARIMAX provides interpretable forecasts in the form of deterministic point estimates. Decision-makers can easily grasp and interpret the forecasted values, making it suitable for scenarios where straightforward predictions are sufficient.
- Model Outputs: SARIMAX provides forecasted values and, if applicable, confidence intervals based on parameter estimates, offering a transparent model structure that allows for clear interpretation of how historical data impacts future predictions.

**DeepAR:**

- Interpretability: DeepAR's probabilistic forecasts offer a more comprehensive understanding of the uncertainty associated with predictions. By presenting forecasts in the form of probability distributions, decision-makers are able to assess the likelihood of different outcomes.
- Model Outputs: The use of probabilistic forecasts with quantiles or probability densities provides valuable information on the inherent uncertainty present in the data. By offering a range of potential outcomes, this approach enhances decision-making under conditions of uncertainty. However, a thorough understanding of the probabilistic framework and model assumptions is necessary to effectively interpret the outputs generated by deep neural networks.

**5. Conclusion**

This paper examines the theoretical contrasts between SARIMAX and DeepAR in the context of time series forecasting. SARIMAX, a traditional statistical method, offers deterministic predictions by modeling linear relationships and seasonal patterns using AR, MA, and I components. This approach provides interpretable outcomes suitable for stable environments characterized by well-defined historical patterns. However,



SARIMAX necessitates manual parameter selection and preprocessing efforts, limiting its capacity to effectively capture intricate non-linear dependencies.

On the other hand, DeepAR leverages deep learning techniques, specifically long short-term memory (LSTM) recurrent neural networks, to provide probabilistic forecasts that account for non-linear data patterns and multiple seasonalities without requiring explicit feature engineering. Its probabilistic approach quantifies uncertainty, facilitating decision-making in dynamic and uncertain situations. However, DeepAR demands considerable computational resources during training and necessitates careful interpretation of its probabilistic forecasts.

The selection of SARIMAX or DeepAR hinges on the specific requirements for forecasting. SARIMAX is best suited for situations in which transparency and ease of understanding are essential, thanks to its clear and uncomplicated model design and deterministic predictions. On the other hand, DeepAR is favored when adaptability, scalability, and the capacity to manage uncertainty are of paramount importance, due to its capacity to capture intricate data patterns and offer probabilistic insights.

Organizations must evaluate their data characteristics, forecasting objectives, and computational resources to determine whether SARIMAX's interpretability or DeepAR's adaptability better aligns with their operational requirements and decision-making processes.

## 6. Future Directions

In the future, it is suggested that research in time series forecasting should focus on combining conventional statistical techniques such as SARIMAX with advanced machine learning methods to leverage their unique strengths and improve accuracy and robustness across a diverse array of datasets. Progress in uncertainty quantification is essential to enhance probabilistic forecasts and refine confidence interval estimation for more effective decision-making under conditions of uncertainty. Additionally, building models that can adapt to evolving data environments and incorporate real-time updates will be crucial for preserving forecasting accuracy in dynamic contexts.

Emerging trends involve improving the interpretability of complex machine learning models, such as DeepAR, to make their predictions more accessible and actionable. However, scalability continues to present a challenge, requiring ongoing optimization of deep learning algorithms, such as DeepAR, to achieve faster training and deployment on large-scale datasets. Future research should also explore innovative neural network architectures specifically designed for time series forecasting, capable of effectively handling long-term dependencies and irregular data patterns. By integrating external knowledge sources and real-time capabilities, these advancements will pave the way for more accurate, adaptable, and scalable forecasting models across various domains and applications.

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