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## Integrating Real-time Data Analytics and Multi-objective Optimization for Enhanced Reservoir Operations: A Review and Framework Proposal

Abiodun Ajala<sup>1</sup>, Josiah Adeyemo<sup>2</sup>, Ismail Salau<sup>3</sup>, Julius Olapade<sup>4</sup>

<sup>1,3,4</sup>Department of Mechanical Engineering, The Polytechnic Ibadan, Nigeria.

Email: [ajala.abiodun@polyibadan.edu.ng](mailto:ajala.abiodun@polyibadan.edu.ng)

<sup>2</sup>University of Washington, Seattle Campus, United States.

Email: [jadeyemo@u.washington.edu](mailto:jadeyemo@u.washington.edu)

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**Abstract** Reservoir operations are vital for managing water resources and meeting various needs, but they face challenges due to complex hydrological structures, abundant operational data, and conflicting conditions. In this comprehensive review, we propose the adoption of two methodologies, the Recurrent Learning Neural Network (RLNN) for real-time data analytics and the Combined Pareto Multi-Objective Differential Evolution (CPMDE) algorithm for multi-objective optimization, to address these challenges. Real-time data analytics play a crucial role in monitoring and understanding reservoir behavior. RLNN, a variant of artificial neural networks, excels in processing sequential data and capturing temporal dependencies. Multi-objective optimization is essential for achieving trade-offs in reservoir operations. CPMDE, a hybrid evolutionary algorithm, combines Pareto-based optimization and differential evolution. It handles conflicting objectives like maximizing water supply, minimizing flood risks, optimizing hydropower generation, and maintaining environmental sustainability. CPMDE explores the trade-off surface, providing decision-makers with a range of Pareto-optimal solutions and alternative strategies for reservoir operations. While RLNN and CPMDE offer individual advantages, their integration into a hybrid RLNN-CPMDE framework creates a comprehensive solution. The proposed hybrid RLNN-CPMDE approach holds great potential for multi-objective real-time reservoir operation optimization. The challenges of reservoir operations require models that address real-time data analytics and multi-objective optimization. RLNN and CPMDE, individually and integrated into a hybrid framework, empower reservoir operators to enhance decision-making processes and achieve efficient and sustainable reservoir operations. These methodologies open avenues for future research, advancing water resource management and reservoir optimization.

**Keywords** multi-objective, reservoir operations, differential evolution, hybrid framework

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### Introduction

Reservoir operations play a crucial role in managing water resources, providing a reliable supply for various purposes such as irrigation, drinking water, hydropower generation, and flood control (A. M. Ikudayisi, 2017). Optimizing reservoir operations is essential to meet the increasing demand for water while balancing competing objectives and addressing environmental concerns. With the growing complexities of reservoir hydrological structures, the exponential growth of operational data, and the presence of conflicting conditions, there is a pressing need for computational models that can effectively handle both real-time data analytics and multi-objective optimization (Apaydin et al., 2020; Ibañez et al., 2021; Olofintoye et al., 2016; Yang et al., 2019).

Traditionally, research in the field of reservoir operations has predominantly focused on either real-time data analytics or multi-objective optimization (Yang et al., 2019). Real-time data analytics involves the monitoring and



analysis of dynamic data related to water levels, inflows, outflows, weather conditions, and other relevant factors. It provides valuable insights into the current state of the reservoir and facilitates timely decision-making. On the other hand, multi-objective optimization aims to find a set of optimal solutions that balance conflicting objectives, such as maximizing water supply, minimizing flood risks, optimizing hydropower generation, and ensuring environmental sustainability (Alakeely & Horne, 2020; Ibañez et al., 2021; A. M. Ikudayisi, 2017; Olofintoye et al., 2016).

In this study, we present a comprehensive review of the existing literature on reservoir operations, focusing on the integration of real-time data analytics and multi-objective optimization. Our goal is to identify suitable methodologies and propose a framework that addresses the challenges associated with reservoir operations in an integrated manner.

To accomplish this, we explore two promising approaches: the Recurrent Learning Neural Network (RLNN) for real-time data analytics and the Combined Pareto Multi-objective Differential Evolution (CPMDE) algorithm for multi-objective optimization. RLNN, a variant of artificial neural networks, excels in processing sequential data and capturing temporal dependencies (Alakeely & Horne, 2020; Apaydin et al., 2020). By analyzing real-time data from diverse sources, RLNN enables reservoir operators to predict and assess the system's behavior accurately. On the other hand, CPMDE, a hybrid evolutionary algorithm, efficiently handles conflicting objectives and identifies a set of Pareto-optimal solutions, offering decision-makers a range of alternative strategies for reservoir operations (Olofintoye et al., 2016).

While RLNN and CPMDE have demonstrated their effectiveness individually, their integration within a hybrid framework holds significant potential for enhancing reservoir operations. We propose a hybrid RLNN-CPMDE approach that incorporates multi-objective optimization principles into RLNN's training process. This integration ensures that the resulting RLNN model generates real-time decisions that are both informed and optimized, considering the trade-offs between different objectives.

By integrating real-time data analytics and multi-objective optimization, our proposed framework aims to improve the efficiency, sustainability, and resilience of reservoir operations. It empowers decision-makers with accurate predictions, comprehensive evaluations, and a range of optimal strategies, enabling them to make informed decisions that balance diverse objectives and adapt to changing conditions.

This study addresses the growing need for computational models that integrate real-time data analytics and multi-objective optimization in reservoir operations. By reviewing the literature and proposing a hybrid RLNN-CPMDE framework, we aim to contribute to the advancement of water resource management and the optimization of reservoir systems. The integration of these methodologies offers promising avenues for future research and practical applications in the field of reservoir operations.

### **Reservoir Performance: Harnessing Neural Networks for Optimal Operation Strategies**

Reservoir operation optimization is a complex task that involves balancing multiple objectives, such as water supply, flood control, hydropower generation, and environmental sustainability. To tackle this challenge, the application of neural networks has gained significant attention due to their ability to handle nonlinear relationships, learn from historical data, and make accurate predictions (Hadiyan et al., 2020). In this section, we delve into the neural network architecture specifically designed for reservoir operation optimization.

One notable neural network architecture that has shown promise in this domain is the Recurrent Learning Neural Network (RLNN). RLNN is a variant of artificial neural networks that excels in processing sequential data and capturing temporal dependencies. Its recurrent structure allows for feedback connections, enabling the network to retain and utilize information from previous time steps (Alakeely & Horne, 2020; Apaydin et al., 2020; Yang et al., 2019). This capability is particularly beneficial in reservoir operations, where historical data plays a crucial role in understanding the system's behavior and making informed decisions.

The architecture of RLNN consists of interconnected layers, including an input layer, one or more hidden layers, and an output layer (Ibañez et al., 2021). Each layer is composed of nodes, also known as neurons, which perform computations on the received data. In the context of reservoir operation optimization, the input layer receives relevant input variables, such as inflow rates, reservoir levels, weather forecasts, and water demand patterns (Hadiyan et al., 2020). These inputs provide crucial information about the current state of the reservoir system.



Training RLNN for reservoir operation optimization involves two key steps: data preparation and model training. In the data preparation phase, historical data related to reservoir levels, inflows, outflows, and other relevant variables are collected and organized. This data is typically divided into training, validation, and testing sets, ensuring that the model is trained on a diverse range of scenarios and can generalize well to unseen data (Zhou et al., 2020).

During the model training phase, RLNN learns from the training data using a process called backpropagation. In backpropagation, the network computes the error between its predictions and the actual observed values and adjusts the connection weights iteratively to minimize this error (Zhou et al., 2020). This process involves optimizing a chosen objective function, such as mean squared error or cross-entropy loss, using optimization algorithms like gradient descent or its variants (Zhou et al., 2020).

Once the RLNN model is trained, it can be deployed for real-time reservoir operation optimization (Hadiyan et al., 2020). By providing real-time input data, such as current reservoir levels, inflows, and weather conditions, the RLNN can generate predictions or decisions for optimal reservoir operations (Hadiyan et al., 2020). These decisions can help reservoir operators make informed choices in real-time, considering various objectives and trade-offs.

### **The Power of Recurrent Learning Neural Networks for Real-Time Reservoir Operation Optimization**

Real-time reservoir operations require efficient computational models that can effectively analyze dynamic data, make accurate predictions, and optimize operational strategies. In recent years, the Recurrent Learning Neural Network (RLNN) has emerged as a powerful tool for optimizing real-time reservoir operations (Ibañez et al., 2021; Yang et al., 2019). In this section, we delve into the application of RLNN and its benefits in enhancing reservoir performance.

RLNN is a variant of artificial neural networks specifically designed to handle sequential data and capture temporal dependencies. This makes it particularly well-suited for analyzing time-varying variables in reservoir systems, such as inflows, outflows, reservoir levels, precipitation, and water demand patterns. By leveraging its recurrent structure, RLNN can retain and utilize historical information, enabling it to capture the dynamic behavior of the reservoir system.

The architecture of RLNN consists of interconnected layers of nodes, each processing and transforming the received data. The input layer of RLNN receives real-time data related to the reservoir system, including current inflow rates, reservoir levels, weather forecasts, and operational constraints. This data serves as valuable input for the network to understand the current state of the reservoir and make informed decisions (Ibañez et al., 2021).

The hidden layers of RLNN play a crucial role in extracting relevant features and patterns from the input data. These layers capture complex relationships and dependencies within the reservoir system, enabling RLNN to learn and model the underlying dynamics (Ibañez et al., 2021). The number of hidden layers and neurons within each layer can be adjusted based on the complexity of the system and the available data.

The output layer of RLNN provides the optimized decisions or predictions for real-time reservoir operations (Ibañez et al., 2021). These decisions can include optimal water release rates, reservoir level adjustments, and operational strategies that aim to balance various objectives, such as maximizing water supply, minimizing flood risks, optimizing hydropower generation, and maintaining environmental sustainability. RLNN generates these decisions by considering the historical data, current inputs, and learned relationships within the reservoir system (Ibañez et al., 2021).

Training RLNN for optimizing real-time reservoir operations involves two key steps: data preparation and model training. In the data preparation phase, historical data encompassing various operational scenarios is collected and organized. This data is typically divided into training, validation, and testing sets to ensure the model's robustness and generalization capabilities. The data may include records of past inflows, reservoir levels, releases, and other relevant variables (Ibañez et al., 2021).

During the model training phase, RLNN learns from the training data using backpropagation and optimization algorithms (Zhou et al., 2020). Backpropagation computes the error between the predicted and actual values, propagating it back through the network to adjust the connection weights iteratively. This iterative process minimizes the error and fine-tunes the network to make more accurate predictions and optimized decisions. Optimization algorithms, such as gradient descent or its variants, are employed to update the network's parameters during the training process (Yang et al., 2019).



Once trained, RLNN can be deployed for real-time reservoir operations optimization (Apaydin et al., 2020). By providing real-time input data, such as current inflows, reservoir levels, weather forecasts, and operational constraints, RLNN generates optimal decisions in real-time. These decisions aid reservoir operators in making timely and informed choices, considering multiple objectives and trade-offs. RLNN's ability to adapt and learn from historical data, combined with its real-time decision-making capabilities, enhances the overall performance of reservoir operations.

### **Optimizing Multi-Objective Reservoir Operations: The Synergy of the Combined Pareto Differential Evolution Algorithm**

Optimizing reservoir operations involves managing multiple conflicting objectives, such as maximizing water supply, minimizing flood risks, optimizing hydropower generation, and ensuring environmental sustainability (Hadiyan et al., 2020). Traditional optimization methods often struggle to handle the complex trade-offs and uncertainties inherent in reservoir systems. To address this challenge, the Combined Pareto Differential Evolution (CPDE) algorithm has emerged as a promising approach for optimizing multi-objective reservoir operations. In this section, we explore the application of CPDE and its advantages in enhancing the performance of reservoir systems.

The CPDE algorithm combines two powerful optimization techniques: Pareto dominance and Differential Evolution (A. Ikudayisi et al., 2018). Pareto dominance is a concept derived from multi-objective optimization, which aims to identify a set of solutions that cannot be improved in any objective without worsening another. Differential Evolution, on the other hand, is a population-based evolutionary algorithm that iteratively searches for optimal solutions by combining mutation, crossover, and selection operations (A. Ikudayisi et al., 2018).

The CPDE algorithm starts by initializing a population of candidate solutions, known as individuals. Each individual represents a potential reservoir operation strategy, comprising decision variables such as release rates, reservoir levels, and operational rules (Adeyemo & Otieno, 2010; Adeyemo & Stretch, 2018; A. Ikudayisi et al., 2018). The algorithm then applies the principles of Pareto dominance to compare and rank the individuals based on their performance across the multiple objectives. This ranking enables the algorithm to identify the best trade-off solutions, forming a Pareto front representing the optimal compromises between different objectives (Adeyemo & Otieno, 2010).

Through a series of iterative generations, the CPDE algorithm evolves the population by applying differential mutation and crossover operations. The mutation operation introduces small perturbations to the individuals, exploring new regions of the search space. The crossover operation combines the information from multiple individuals to generate offspring with potentially better performance. These operations mimic the natural evolutionary processes of variation and recombination, allowing the algorithm to search for improved solutions (Adeyemo & Otieno, 2010).

The key advantage of the CPDE algorithm lies in its ability to handle the conflicting objectives of reservoir operations. By maintaining a diverse population of solutions on the Pareto front, CPDE offers decision-makers a range of alternative strategies, each representing a different trade-off between the competing objectives. This flexibility allows reservoir operators to select the most suitable solution based on their priorities, stakeholder preferences, and current system conditions.

Training the CPDE algorithm for multi-objective reservoir operations optimization requires careful consideration of several factors. The selection of objective functions that represent the desired reservoir performance is crucial. These objective functions can be customized based on the specific objectives and constraints of the reservoir system under consideration. Additionally, appropriate parameter settings for mutation rates, crossover probabilities, and population size need to be determined through experimentation and fine-tuning to achieve optimal performance (A. Ikudayisi et al., 2018).

The deployment of the CPDE algorithm in real-world reservoir operations involves integrating it into decision support systems. By providing real-time input data, such as current reservoir levels, inflows, demand patterns, and environmental constraints, the CPDE algorithm generates a set of Pareto-optimal solutions. Reservoir operators can then analyze and evaluate these solutions to make informed decisions based on the current system conditions and objectives.



The Combined Pareto Differential Evolution (CPDE) algorithm has emerged as a powerful approach for optimizing multi-objective reservoir operations. By combining the principles of Pareto dominance and Differential Evolution, CPDE enables the identification of optimal trade-off solutions that balance competing objectives. The algorithm's ability to provide a diverse range of alternatives empowers decision-makers with greater flexibility and informed decision-making capabilities. Further research and advancements in CPDE and its integration into decision support systems hold significant potential for enhancing the performance and sustainability of reservoir systems.

### **CPMDE multi-objective optimization**

The Combined Pareto Multi-Objective Differential Evolution (CPMDE) algorithm is a powerful optimization technique designed to address multi-objective optimization problems. It combines the principles of Pareto dominance and differential evolution to efficiently explore the solution space and find a set of solutions that represent the optimal trade-offs between conflicting objectives (Olofintoye et al., 2016).

Multi-objective optimization involves optimizing multiple objectives simultaneously, where improving one objective may lead to a deterioration in others (Olofintoye et al., 2014). Traditional optimization methods often focus on a single objective and fail to capture the complexity of real-world problems with multiple conflicting objectives.

The CPMDE algorithm overcomes this limitation by employing a population-based approach and maintaining a diverse set of solutions. It starts by initializing a population of candidate solutions randomly within the feasible solution space (Olofintoye et al., 2014). Each candidate solution is represented as a vector of decision variables.

The algorithm proceeds through a series of iterations, commonly referred to as generations. In each generation, the CPMDE algorithm performs the following steps (Olofintoye et al., 2014):

**Mutation:** A mutation operation is applied to perturb the population. This is achieved by adding a small perturbation to each candidate solution, generating a new trial solution.

**Crossover:** A crossover operation is performed to combine the information from the trial solution with the original candidate solution. This step generates an intermediate solution that represents a potential improvement over the current solution.

**Selection:** The intermediate solution is then compared to the original candidate solution using Pareto dominance. Pareto dominance determines if one solution is better than another across multiple objectives without being worse in any objective. If the intermediate solution dominates the original candidate solution, it replaces it in the population. Otherwise, the original candidate solution is retained.

By repeating these steps for a predefined number of generations, the CPMDE algorithm gradually improves the quality of the population by continuously exploring the solution space and maintaining a diverse set of non-dominated solutions. This results in a set of solutions known as the Pareto front, representing the optimal trade-offs between the conflicting objectives.

The CPMDE algorithm offers several advantages for multi-objective optimization. Firstly, it effectively balances exploration and exploitation by combining the global search capability of differential evolution with the Pareto dominance-based selection (Olofintoye et al., 2014). Secondly, it can handle problems with a large number of objectives and decision variables (Olofintoye et al., 2014). Lastly, it does not require any problem-specific knowledge or assumptions, making it a versatile approach applicable to various domains (Olofintoye et al., 2014).

### **Applications of CPMDE to reservoir operation**

The application of the Combined Pareto Multi-Objective Differential Evolution (CPMDE) algorithm to multi-objective reservoir operation presents an effective approach for optimizing the management and utilization of water resources in reservoir systems. Reservoir operation involves making decisions on the release of water from a reservoir to meet various objectives such as water supply, flood control, hydropower generation, irrigation, and environmental conservation.

CPMDE offers a powerful tool to tackle the inherent complexity of reservoir operation problems, where multiple conflicting objectives need to be considered simultaneously. By utilizing the principles of Pareto dominance and differential evolution, CPMDE can efficiently explore the trade-offs between conflicting objectives and provide a set of non-dominated solutions, known as the Pareto front (Olofintoye et al., 2014).





The CPMDE algorithm can be applied to optimize various objectives in reservoir operation, including:

**Water Supply:** The algorithm can optimize the release policies to ensure an adequate and reliable water supply for different purposes such as municipal water supply, industrial use, or agricultural irrigation. By considering factors such as reservoir storage levels, downstream water demand, and future inflow forecasts, CPMDE can help identify release strategies that balance water supply requirements with other objectives (Olofintoye et al., 2014).

**Flood Control:** Reservoirs play a crucial role in mitigating floods by regulating the downstream flow. CPMDE can optimize the reservoir release patterns during flood events to minimize the downstream flood risk while considering other objectives. It can determine the optimal release rates and timings to manage flood peaks and reduce potential damages to downstream areas (Adeyemo & Olofintoye, n.d.).

**Hydropower Generation:** Many reservoir systems are used for hydropower generation. CPMDE can optimize the operation rules and release policies to maximize the hydropower generation while taking into account other objectives such as maintaining a minimum environmental flow or meeting downstream water demands (Adeyemo & Stretch, 2018).

**Environmental Conservation:** Reservoir operation should also consider the ecological needs of downstream ecosystems (Enitan et al., 2014, 2015). CPMDE can incorporate environmental objectives such as maintaining minimum flows, preserving habitat quality, or preventing water quality degradation. By finding trade-offs between conflicting objectives, CPMDE can identify operating strategies that strike a balance between water use and ecological sustainability.

The application of CPMDE to multi-objective reservoir operation provides decision-makers with a set of Pareto-optimal solutions that represent the trade-offs between various objectives. These solutions enable decision-makers to explore different management options and make informed decisions based on their preferences and priorities. By considering multiple objectives simultaneously, CPMDE can help find more sustainable and robust reservoir operation strategies.

## Conclusion

In conclusion, this paper has presented a comprehensive review and proposed a framework for integrating real-time data analytics and multi-objective optimization techniques to enhance reservoir operations. The synergistic utilization of neural networks, specifically Recurrent Learning Neural Networks (RLNN), and the Combined Pareto Differential Evolution (CPDE) algorithm has demonstrated great potential in unlocking reservoir performance and addressing the challenges associated with real-time decision-making and multi-objective optimization. The proposed framework, which combines real-time data analytics with multi-objective optimization techniques, offers a systematic approach to improving reservoir operations. By integrating RLNN and the CPDE algorithm, reservoir operators can make well-informed decisions based on real-time data, historical information, and trade-off analyses. The framework facilitates the efficient allocation of water resources, minimizes operational risks, maximizes performance, and ensures the long-term sustainability of reservoir systems.

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